

Two Level Structure for Reactive Power in Deregulated Electricity Markets

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Abstract— The main objective of this Paper is to propose an two level structure for reactive power in deregulated electricity markets. Considering the various issues associated with the existing policies and practices for reactive power management and payment mechanisms, a competitive two level reactive power management structure is proposed. This structure is based on the separation of reactive power management into two distinct time-frames, i.e. a reactive power procurement stage carried out on a seasonal basis, and a reactive power dispatch stage that determines the reactive power levels in “real-time”.

Index Terms— Reactive power management, Deregulated electricity markets, Reactive power procurement, Reactive power dispatch.

1 INTRODUCTION

THE Reactive power is tightly related to bus voltages throughout a power network, and hence reactive power services have a significant effect on system security. Insufficient reactive power supply can result in voltage collapse, which has been one of the reasons for some recent major blackouts; for example, the US-Canada Power System Outage Task Force states in its report that insufficient reactive power was an issue in the August 2003 blackout, and has recommended strengthening the reactive power and voltage control practices in all North American Electric Reliability Council (NERC) Regions [1]. In deregulated electricity markets, the Independent System Operator (ISO) is responsible for the provision of additional services that are necessary to support the transmission of electrical energy while maintaining secure and reliable operation of the power system; these services are referred to a *ancillary services*. According to the Federal Energy Regulatory Commission (FERC) Order No.888, reactive power supply and voltage control from generators is one of six ancillary services that transmission providers must include in an open access transmission tariff [2]. FERC Order 2003[3] further states that a reactive power provider should not be financially compensated when operating within a power factor range of 0.95 lagging and 0.95 leading, but an Independent System Operator (ISO) may change this range at its discretion. System operators and researchers have been looking for appropriate mechanisms for reactive power provision in the context of deregulation [4],[5],[6],[7].

However, there are several issues concerning the existing provision policies and payment mechanisms for reactive power services that impede the full development of a competitive

market. Hence, this paper proposes a possible market structure and related techniques to address some of the main issues associated with reactive power provision in competitive electricity markets.

2 ISSUES IN EXISTING REACTIVE POWER MANAGEMENT POLICIES

2.1 Lost Opportunity Cost

It is well accepted that the principal function of a synchronous generator is to generate real power to meet the demand of the system[8]. Under certain circumstances, usually arising from critical system conditions, the ISO may request or instruct a generator to increase its reactive power output, which may require a reduction in its active power output, thereby affecting market conditions.

2.2 Reactive Power Payment Mechanisms

An important issue that arises with regards to reactive power markets is the choice of an appropriate payment mechanism. Should it be a market-based auction mechanism where the suppliers provide their reactive power bids to the ISO, which in turn determines the best reactive power offer using an appropriate objective function? If so, should it then be a uniform price market for reactive power with a single reactive power price for the whole system, or a zonal level reactive power auction market where the system is divided in zones and separate reactive power prices are determined for each zone?

2.3 Optimal Provision For Reactive Power Services

In a competitive electricity market, reactive power provision by the ISO should be achieved in an optimal manner. The question that arises here is: what is the best optimization criterion to be adopted by the ISO? In other words, what is the optimization objective that the ISO should be seeking to determine the system reactive power schedules? Should it be system loss minimization, as it has been the usual practice, or minimization of reactive power costs?

2.4 Energy Price Volatility

It has been the general experience of market operators and

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ISOs that energy prices can be highly volatile under certain system conditions, such as demand spikes or outages. In a short-term operational time-frame, volatile energy market conditions would certainly have an impact on reactive power procurement and dispatch procedures.

2.5 Reactive Power Market Power

In a reactive power market, it is certainly possible that some “well-located” suppliers may try to game the price offers by submitting excessively high price offers, or withholding reactive power supply in an attempt to increase the reactive power market price to their advantage[9],[10],[11].

3 TWO SETTLEMENT REACTIVE POWER MANAGEMENT FRAMEWORK

A two-settlement reactive power management scheme is proposed here comprising two major activities at different hierarchical levels as depicted in Fig. 1. The first level consists of a long-term procurement market on a seasonal basis. In the second level, the ISO carries out the actual reactive power dispatch in a time frame of 30 minutes to 1 hour ahead of realtime, by solving an OPF with an appropriate objective function.

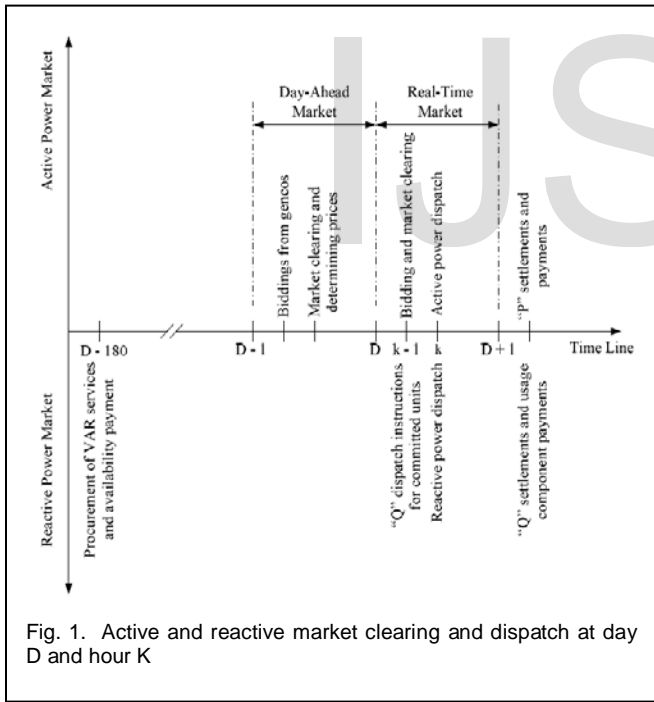


Fig. 1. Active and reactive market clearing and dispatch at day D and hour K

Figure 1 illustrates how the active and reactive power markets can be decoupled from each other, placing them in different operating time frames, so that the ISO does not handle a reactive power auction in the same time frame as that of a real power auction. This minimizes the risk that might arise from price volatility, and thus help reduce market inefficiencies.

4 PROPOSED LONG TERM REACTIVE POWER PROCUREMENT MODEL

As mentioned earlier, the first level in the proposed hierarchical reactive power management scheme is the design of a procurement market model. The objective of the ISO in this case is essentially to define and procure adequate long-term reactive power supplies for the system. The proposed procurement market would work as follows (see Fig. 2):

The ISO calls for reactive power offers from the reactive power providers. The structure of these offers should ideally reflect their cost of providing reactive power; this issue is discussed in more detail below. Based on the received offers, the

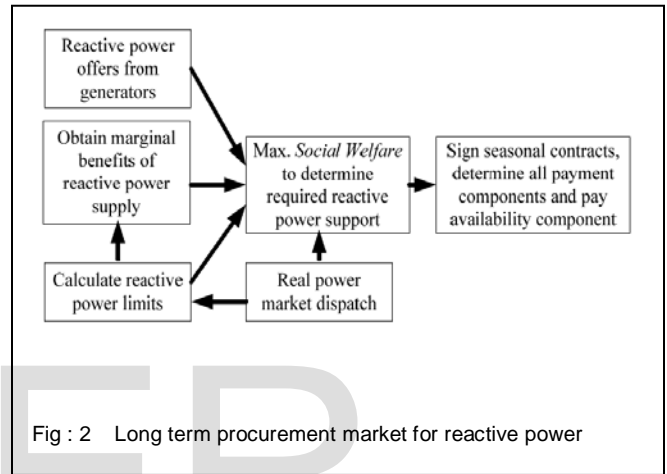


Fig : 2 Long term procurement market for reactive power

ISO carries out an auction settlement, i.e. solves an optimization model to maximize a societal advantage function (SAF) subject to system constraints that include system security. This procurement market settlement, i.e. the solution of the optimization model, yields a set of contracted generators, as well as the price components of reactive power. The contracted providers will have a seasonal obligation for reactive power provision, and receive an availability payment.

4.1 Determine Reactive Power Ancillary Service Limits

When real power and terminal voltage are fixed, the armature and field winding heating limits determine the reactive power capability of a generator. These limits are illustrated in Fig. 3, where V_t is the voltage at the generator terminal bus, I_a is the armature current, E_f is the excitation voltage, X_s is the synchronous reactance, and P_G and Q_G are the real and reactive power outputs of the generator, respectively. The generator’s MVA rating is the point of intersection of the two curves, and therefore its real power rating is given by P_{GR} . At an operating point A, with real power output P_{GA} such that $P_{GA} < P_{GR}$, the limit on Q_G is imposed by the generator’s field winding heating limit; whereas, when $P_{GA} > P_{GR}$, the limit on Q_G is imposed by the generator’s armature winding heating limit.

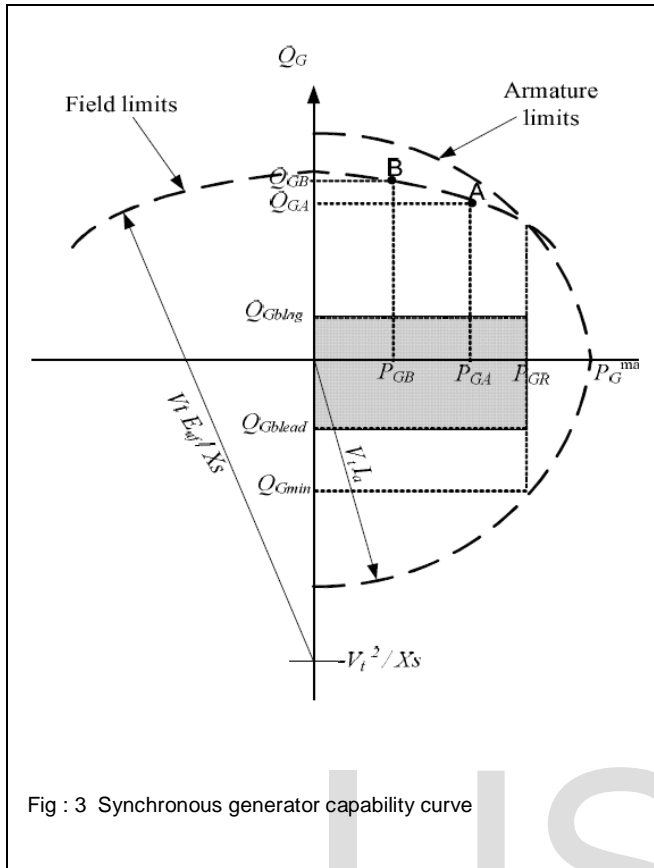


Fig : 3 Synchronous generator capability curve

Three regions for reactive power generation can be identified in Fig. 3. In Region I ($Q_{Gmin} = Q_G = Q_{G1} = 0$), the generators are required to mandatorily provide a base leading reactive power support (Q_{Gblead} to 0). Any reactive power provided beyond Q_{Gblead} is eligible for an under-excitation payment component as an ancillary service.

In the same way, in Region II ($0 = Q_G = Q_{G2} = Q_{GA}$), the mandatory lagging reactive power requirement is from 0 to Q_{Gblag} , and any reactive power provision beyond Q_{Gblag} is recognized as an ancillary service, and thus eligible for a payment for the increased losses in the windings; this payment component is referred to as cost of loss payment. The shaded area in Fig. 3 represents the mandatory base reactive power provision range set by the system operator.

In Region III ($Q_{GA} = Q_G = Q_{G3} = Q_{GB}$), any reactive output increase requested by the ISO beyond Q_{GA} will require a decrease in active power generation, and hence an opportunity cost payment to the reactive power service providers is expected.

4.2 Marginal Benefits of Reactive Power Supply With Respect To Generation Cost

Based on this optimization of reactive power which gives Lagrange multipliers that represent the marginal benefit/contribution of each reactive source, SAF is maximized. The classical concept of social welfare from economic theory is extended to formulate a reactive power SAF (Societal Ad-

vantage Function) which is basically determination of aggregate system benefits accrued from reactive power services minus the expected payment by the ISO.

4.3 Reactive Power Offers From Generators

The different reactive power cost components discussed form the basis for the procurement procedure proposed here. Hence, the reactive power price offers to be submitted by generators should comprise the following three parts (Fig. 4) :

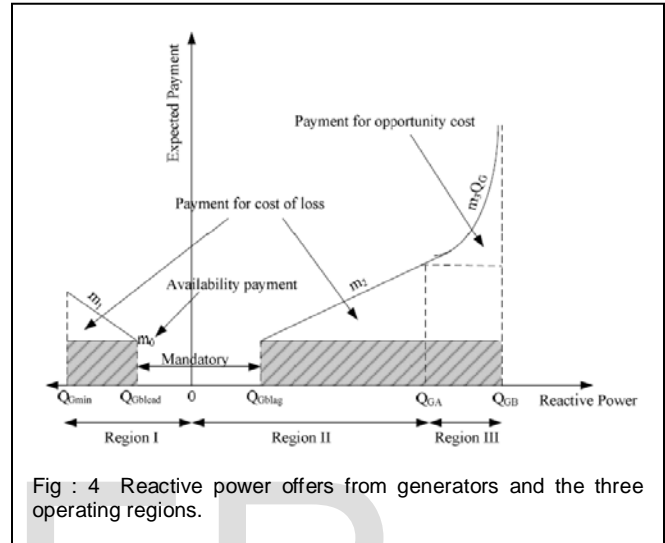


Fig : 4 Reactive power offers from generators and the three operating regions.

Availability price offer (m_0 , \$): A fixed component to account for that portion of a supplier's capital cost that can be attributed to reactive power production.

Cost of loss offer (m_1, m_2 , \$/Mvar): An assumed linearly varying component to account for the increased winding losses as reactive power output increases, in the under and over-excitation ranges respectively [10].

Opportunity offer (m_3 , \$/Mvar/Mvar): A quadratic component to account for the lost opportunity cost when a supplier is constrained from producing its scheduled real power in order to increase its reactive power production.

4.4 Reactive Power Prices

Uniform price market, where all selected participants are paid a uniform price, which is the price of the highest accepted offer. The uniform price markets provide an incentive to participants to bid their true costs and hence such auctions promote competition. Zonal uniform price mechanism for reactive power markets would reduce the impact of market power exercised by certain gaming generators, and should hence restrict them only to their given zones.

4.5 Societal Advantage Function Maximization

Once the reactive power ancillary service limits and the marginal benefits of each provider with respect to generation cost are determined, and reactive power offers are received, the ISO is in a position to carry out a procurement market settle-

ment where its sole objective is to maximize a societal advantage function. The proposed SAF is formulated on a zonal basis and can be expressed as follows:

$$\begin{aligned}
 SAF_k = & -\sum_{g \in K} \rho_{ok} - \sum_{g \in K} (C_L |\mu_g| - \rho_{1k}) (Q_{G1g} - Q_{Gblead_g}) \\
 & + \sum_{g \in K} (C_L |\lambda_g| - \rho_{2k}) (Q_{G2g} - Q_{Gblag_g}) \\
 & + \sum_{g \in K} \left((C_L |\gamma_g| - \rho_{2k}) (Q_{G3g} - Q_{Gblag_g}) \right) \\
 & - 0.5 \rho_{3k} (Q_{G3g} - Q_{GA_g})^2
 \end{aligned} \tag{1}$$

In (1), the subscript g denotes a generator in the system, while K refers to the set of generators in zone k , considering that the system is divided into voltage control zones. The variables ρ_{1k} (in \$/Mvar) and ρ_{2k} (in \$/Mvar) are the under- and over-excitation prices for reactive power in zone k , respectively; similarly ρ_{3k} (in \$/Mvar/Mvar) is the zonal uniform opportunity price component. The variable ρ_{ok} (in \$) is the zonal availability price component. The constant C_L is a "loadability" cost parameter (in \$/MWh) denoting the economic worth of increasing the system loadability. λ , γ and μ are the Lagrange multipliers obtained from optimization model of marginal benefits of reactive power supply with respect to generation cost. Q_{Gblag} , Q_{Gblead} are the mandatory lagging and leading reactive power provided by generator. Q_{G1g} , Q_{G2g} and Q_{G3g} are regions of reactive power as shown in fig4.

5 PROPOSED SHORT TERM REACTIVE POWER DISPATCH MODEL

The proposed schematic procedure is shown in Figure 5 for short term dispatch of reactive power services. In this model, the ISO carries out the reactive power dispatch in a time frame of one hour to half-hour ahead of real-time by solving an OPF that minimizes the cost of reactive power provision from generators, the cost of active power rescheduling, and the cost of real power balance, subject to power flow and security constraints.

The payments to the service providers are calculated post real-time operation, based on the actual usage and dispatch requested by the ISO aggregated over a period of time.

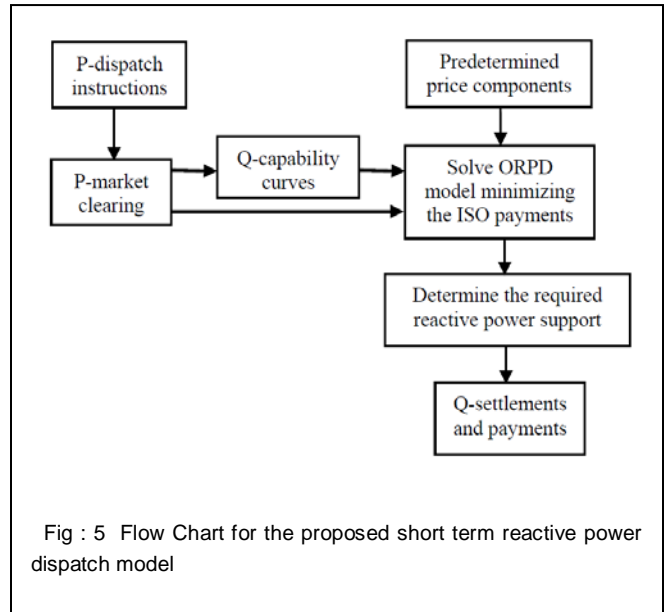


Fig : 5 Flow Chart for the proposed short term reactive power dispatch model

5.1 Reactive Power Dispatch Model

Reactive power production capability of a generator essentially depends on the current state of real power generation (P_G). Hence, prior knowledge of P_G is essential in order to calculate reactive capability limits. The values of P_G for the generators are obtained from real power market clearing information.

A cost-based Q-dispatch model is proposed here, which takes into account both economic and technical issues associated with reactive power service provisions in a competitive electricity market. The model is formulated as follows:

$$\begin{aligned}
 \text{Min} \quad & \sum_g \left(\rho_{0g} + \rho_{2g} \cdot Q_{G2g} - \rho_{1g} \cdot Q_{G1g} \right. \\
 & \left. + \rho_{2g} \cdot Q_{G3g} - 0.5 \rho_{3g} \cdot (Q_{G3g} - Q_{GA_g})^2 \right) \\
 & + \sum_g \rho_{B1} \cdot P_{B1g} + \sum_g \rho_{B2} \cdot P_{B2g}
 \end{aligned} \tag{2}$$

$$\begin{aligned}
 \text{s.t.} \quad & P_{G10} - \Delta P_{G1} + P_{B1} - P_{D1} \\
 & = \sum_j V_i V_j Y_{ij} \cos(\theta_{ij} + \delta_j - \delta_i)
 \end{aligned} \tag{3}$$

$$Q_{Gi} - Q_{Di} = -\sum_j V_i V_j Y_{ij} \sin(\theta_{ij} + \delta_j - \delta_i) \quad (4)$$

$$V_i^{\min} \leq V_i \leq V_i^{\max} \quad (5)$$

$$|P_{ij}| \leq P_{ij}^{\max} \quad (6)$$

$$\Delta P_{Gi} \leq c_i P_{Goi} \quad (7)$$

$$P_{B1,2i}^{\min} \leq P_{B1,2i} \leq P_{B1,2i}^{\max} \quad (8)$$

$$P_{Gxg} = \begin{cases} \sqrt{(V_t I_a)^2 - Q_{Gg}^2} & \text{if } Q_{Gg} \geq Q_{GAg} \text{ \& } P_{Ggo} > P_{Rg} \\ \sqrt{\left(\frac{V_t E_{af}}{X_s}\right)^2 - \left(Q_G + \frac{V_t^2}{X_s}\right)^2} & \text{if } Q_{Gg} \geq Q_{GAg} \text{ \& } P_{Ggo} < P_{Rg} \\ P_{Gog} & \text{otherwise} \end{cases} \quad (9)$$

$$P_{Gog} - P_{Gg} = \Delta P_{Gg} \quad (10)$$

$$P_{Goi} - \Delta P_{Gi} + P_{Bi} \leq P_{Gi}^{\max} \quad (11)$$

$$Q_{Gg}^{\min} \leq Q_{G1g} \leq Q_{Gbleadg} \quad (12)$$

$$Q_{Gblag_g} \leq Q_{G2g} \leq Q_{GAg} \quad (13)$$

$$Q_{GAg} \leq Q_{G3g} \leq Q_{GBg} \quad (14)$$

$$Q_{G1g} \cdot Q_{G2g} = 0 \quad (15)$$

$$Q_{G2g} \cdot Q_{G3g} = 0 \quad (16)$$

$$Q_{G1g} \cdot Q_{G3g} = 0 \quad (17)$$

$$Q_{Gg} = Q_{G1g} + Q_{G2g} + Q_{G3g} \quad (18)$$

where

ρ_{B1} : Price of the upward balance services P_B in \$/MW.

ρ_{B2} : Price of the downward balance services P_B in \$/MW.

ρ_{og} : Availability price for generator g in \$.

ρ_{1g} : Price of Losses in the under-excitation region for generator g in \$/MVar.

ρ_{2g} : Price of losses in the over-excitation region for generator g in \$/MVar.

ρ_{3g} : Loss of opportunity price for generator g in \$/MVar/MVar.

ΔP_{Gi} Reduction in active power at bus i due to increase in reactive power beyond heating limits.

P_{Goi} : Pre-determined active power dispatch at bus i .

P_{B1} : Upward balance service at bus i .

P_{B2} : Downward balance service at bus i .

c_i : Maximum allowed level of active power reduction at bus i .

P_{Gxg} : New active power dispatch for generator g .

The proposed reactive power dispatch model is supposed to run in a 30 min to 1 h window, and the solution yields the required reactive power support that minimizes the payment

by the ISO, while considering system security constraints represented through voltage limits (5) and transmission line power flow limits (6).

6 CONCLUSION

Based on the current practices for reactive power provision by various ISOs in competitive electricity markets, this paper has proposed a streamline reactive power market structure. The proposed market design consists two stages, namely, procurement of reactive power resources on a seasonal basis, and a real-time reactive power dispatch. The proposed procurement market model, which is the main focus of this paper, is based on at first level with two-step optimization process; the first step consists of the determination of the marginal benefits of reactive power with respect to generation cost, which are then used in the second step to maximize a reactive power societal advantage function (SAF) considering bids from service providers. In the second level, reactive power dispatch which is basically short term management is considered based on first result.

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